



Forming An Optimal Portfolio by Applying the Data Envelopment Analysis (DEA) Approach Based on The Single Index Model

Andre Kussuma Adiputra^{1,a)}, V. Wiratna Sujarweni^{1,b)}, Poly Endrayanto Eko
Christmawan^{1,c)}

¹*Department of Accounting, Universitas Respati Yogyakarta, Yogyakarta, Indonesia*

^{a)} Corresponding author: andre_adiputra@respati.ac.id

Abstract. The study aims to determine the optimal portfolio formation using the Data Envelopment Analysis (DEA) approach based on the Single Index Model. The significance of this research lies in providing investors with an effective tool for maximizing returns while minimizing risk through portfolio diversification. The DEA method is applied to measure the efficiency of selected stocks listed on the Indonesian Stock Exchange between 2020 and 2023. By utilizing technical efficiency, the study evaluates stocks to identify efficient Decision-Making Units (DMUs) for portfolio candidates. The Single Index Model, developed by William Sharpe, is used to calculate expected returns and associated risks. The research uses purposive sampling, focusing on companies in the industrial sector. Monthly stock prices, dividends, and macroeconomic data such as the Indonesian Stock Exchange Index (IHSG) and Bank Indonesia Certificate (SBI) interest rates serve as inputs. Using DEA-CCR and DEA-BCC models, efficient stocks are selected based on efficiency scores. The results highlight 11 stocks as optimal portfolio candidates, including Astra International (ASII) and Perma Plasindo (BINO). The portfolio provides an expected monthly return of 0.0211213 with a standard deviation of 0.026621, indicating potential outperformance relative to the market index.

Keywords: Optimal Portfolio, Data Envelopment Analysis, Single Index Model

INTRODUCTION

Optimal Portfolio, Data Envelopment Analysis, Single Index Model Investment is the activity of allocating funds or assets into various financial instruments, properties, or businesses to generate future returns. Investors, particularly in the Indonesian capital market, pursue a variety of goals when making investments [1]. These goals include capital growth, where investors aim for their investments to increase in value over time, thus building long-term wealth. Additionally, investors seek regular income through dividends from stocks or interest from bonds. Beyond financial gains, investment also serves as a means to hedge against inflation [2], as expected returns from investments often outpace or at least match inflation rates. Furthermore, [3], lowers the potential for substantial losses from market volatility.

Diversification has become a fundamental strategy in investment, reducing asset-specific risks and enhancing profit opportunities [4]. It allows investors to balance losses in one asset class with gains in another, thereby protecting their portfolios. Investors are also able to capitalize on different phases of the economic cycle, with certain asset classes performing better during different economic conditions. This further underscores the need for a well-diversified portfolio that can mitigate risk while maintaining the potential for returns [5].

However, investment decisions are primarily influenced by two key aspects: return and risk. [6]. A higher return is generally desirable, but it must be weighed against

the associated risks. Rational investors aim to construct optimal portfolios that strike the right balance between expected return and acceptable risk levels, allowing them to meet their long-term investment objectives in a stable and calculated manner [7].

The challenge, however, lies in determining which portfolio configuration is best, given the vast array of available investment options. This leads to the question: which portfolio should an investor choose to achieve the best balance of risk and return? [8], who proposed the idea of an efficient portfolio that maximizes return for a given level of risk, or minimizes risk for a given return. His model, known as the mean-variance efficient frontier, laid the foundation for modern financial theory [9].

To enhance the selection process for efficient stocks in portfolio formation, techniques such as Data Envelopment Analysis (DEA) have been employed to compare the efficiency of various assets by considering their inputs and outputs [10]. Furthermore, the Single Index Model developed by William Sharpe adds another dimension to portfolio optimization

METHODS

The optimal portfolio is a portfolio selected by investors from a set of efficient portfolios, based on their preferences regarding risk and expected return. An efficient portfolio is determined by its ability to provide higher returns at the same level of risk or to offer lower risk at the same return [6]. In stock investments, returns can consist of dividends and capital gains, while risk is calculated through variance or standard deviation [11]. Risk is divided into two categories: systematic risk, influenced by market factors and cannot be eliminated through diversification, and unsystematic risk, which can be mitigated through diversification [12].

The Single Index Model, developed by William Sharpe, simplifies the analysis of portfolio return and risk by linking stock returns with the market index [13]. Additionally, the Data Envelopment Analysis (DEA) method is used to measure the relative efficiency of a portfolio by comparing output (expected return) against input (risk level) [14]. The DEA model measures technical efficiency using various versions, such as DEA-CCR, which assumes constant returns to scale, and DEA-BCC, which considers variable returns to scale [15].

This study uses a sample of industrial sector companies listed on the Indonesia Stock Exchange (IDX) from 2020 to 2023. Purposive sampling is employed to select companies with complete data related to stock prices, dividends, the IDX Composite Index (IHSG), Bank Indonesia Certificate (SBI) interest rates, and annual financial reports [16]. The input-output variables analyzed include standard deviation, beta, DER, EPS, return, BV, PBV, ROE, ROA, PER, and NPM, with standard deviation, beta, DER, and PER as input variables, and the rest as output variables [17]. The steps taken include calculating return, risk, beta coefficient, and various other financial ratios to determine the technical efficiency and scale of stocks using the DEA-CCR and DEA-BCC models with the aid of LINGO 11.0 software [18].

After identifying efficient stocks, the optimal portfolio is constructed using the Single Index Model. Excess return to beta (ERB) is calculated as the difference between expected return and risk-free return, followed by the calculation of the cut-off rate (C_i) to determine which stocks will be included in the optimal portfolio [8], [19]. The proportion of funds for each stock in the portfolio is calculated based on the level of risk, and the

portfolio's risk and expected return are then calculated to assess the overall performance of the constructed portfolio[20].

RESULTS AND DISCUSSION

Determination of Stocks as Portfolio Candidates through the Decision-Making Units (DMU) Efficiency Approach Based on the Single Index Model

The steps used to determine stocks as portfolio candidates are as follows:

1. Calculation of Return and Expected Return of Individual Stocks

The results of the investment are measured from the return obtained in a certain period. For example, the return for Astra International Tbk for the March 2023 period was 0.090164, or a short return of 9.01% while the April 2023 stock return showed a figure of 0.23333 or a short return of 23.33%. This shows that in the April 2023 period, the stock experienced a fairly high increase in the level of profit.

After obtaining the return of each stock, the expected return of each stock will be calculated which is presented in Table 1.

| KODE | E(Rt) | KODE | E(Rt) | KODE | E(Rt) | KODE | E(Rt) |
|------|-------------|--------|---------|------|---------|------|---------|
| AMFG | 0,02171381 | DYAN | -0,0021 | KIAS | -0,0493 | SCCO | 0,01325 |
| APII | -0,00419343 | GPSO | -0,0103 | KOBX | -0,019 | SINI | 0,01646 |
| ARKA | 0 | HOPE | 0,01833 | KOIN | -0,027 | SKIN | -0,0292 |
| ARNA | 0,019016892 | IBFN | -0,0641 | KONI | -0,0555 | SOSS | 0,00678 |
| ASGR | 0,031881432 | ICON | -0,0138 | KUAS | 0,02258 | SPTO | 0,09155 |
| ASII | 0,106165975 | IKAI | 0 | LABA | -0,052 | TIRA | 0,05764 |
| BHIT | -0,01054639 | IMPACT | -0,017 | LION | -0,0165 | TOTO | 0,06428 |
| BINO | 0,006261015 | INDX | -0,0615 | MARK | 0,06622 | UNTR | 0,26312 |
| BLUE | 0,117231897 | INTA | -0,027 | MDRN | -0,1205 | VOKS | 0,04154 |
| BNBR | 0,656351284 | JECC | -0,0265 | MFMI | 0,02084 | ZBRA | -0,0146 |
| CAKK | -0,00064415 | JTPE | 0,10168 | MLIA | 0,04096 | | |
| CCSI | -0,03044855 | KBLI | 0,02037 | NTBK | 0,01405 | | |
| CTTH | -0,06944444 | KBLM | 0,03935 | PADA | -0,1016 | | |

Table 1. Stock Expected Return

2. Calculation of Individual Stock Risk

Risk is the magnitude of the deviation between the expected return and the actual return. The tool used as a measure of this spread is the variance or standard deviation.

| KODE | Risiko (oi) | KODE | Risiko (oi) | KODE | Risiko (oi) | KODE | Risiko (oi) | KODE | Risiko (oi) |
|------|-------------|------|-------------|------|-------------|-------|-------------|------|-------------|
| AMFG | 0,00428915 | CCSI | 0,00313 | JECC | 0,00951 | MAR K | 0,01378 | TIRA | 0,2103 |
| APII | 0,00027237 | CTTH | 0,04083 | JTPE | 0,01398 | MDRN | 0,05055 | TOTO | 0,00097 |
| ARKA | 0 | DYAN | 0,02024 | KBLI | 0,00304 | MFMI | 0,00506 | UNTR | 0,01664 |

| | | | | | | | | | |
|------|----------------|------|-------------|----------|-------------|------|-------------|------|-------------|
| ARNA | 0,0027022 3 | GPSO | 0,0259 4 | KBL M | 0,0079 5 | MLIA | 0,0029 4 | VOKS | 0,0054 2 |
| ASGR | 0,0031075 6 | HOPE | 0,0037 | KIAS | 0,0694 6 | NTBK | 0,0211 4 | ZBRA | 0,0003 1 |
| ASII | 0,0037053 | IBFN | 0,1423 9 | KOBX | 0,0101 2 | PADA | 0,0305 3 | | |
| BHIT | 0,0006191 8 | ICON | 0,0025 7 | KOIN | 0,0146 6 | SCCO | 0,0014 9 | | |
| BINO | 0,0035605 5 | IKAI | 0 | KONI | 0,0693 9 | SINI | 0,0984 6 | | |
| BLUE | 0,0036088 9 | IMPC | 0,0746 7 | KUAS | 0,0011 3 | SKRN | 0,0789 7 | | |
| BNBR | 6,6938459 4 | INDX | 0,0113 4 | LABA | 0,0032 9 | SOSS | 0,0115 4 | | |
| CAKK | 0,0138511 1 | INTA | 0,0080 4 | LION | 0,0174 5 | SPTO | 0,0004 5 | | |

Tabel 2. Individual Stock Risk

3. Beta Risk Coefficient Calculation

To obtain the beta risk coefficient value of each stock, it is necessary to calculate the market return variance and stock-return covariance first. The market return variance value is obtained, which is presented in table 3 and the beta risk coefficient value of each stock can be calculated, the results of which are presented in table 4.

| KODE | Covarian Saham dengan IHSG | KODE | Covarian Saham dengan IHSG | KODE | Covarian Saham dengan IHSG | KODE | Covarian Saham dengan IHSG |
|------|----------------------------|------|----------------------------|------|----------------------------|------|----------------------------|
| AMFG | 0,000596184 | DYAN | -0,000826016 | KIAS | 0,001618464 | SCCO | -0,0003 |
| APII | 2,63E-05 | GPSO | 0,001034417 | KOBX | 0,001083156 | SINI | -0,0008 |
| ARKA | 0 | HOPE | 0,000400264 | KOIN | 0,00172951 | SKRN | 0,0006 |
| ARNA | 0,000374908 | IBFN | -0,003592429 | KONI | 0,001889546 | SOSS | -0,0004 |
| ASGR | 0,000438476 | ICON | -0,00011472 | KUAS | -4,53E-05 | SPTO | 0,00021 |
| ASII | 0,000430192 | IKAI | 0 | LABA | 0,000469663 | TIRA | -0,0013 |
| BHIT | -3,94E-05 | IMPC | -3,83E-05 | LION | -0,000738119 | TOTO | 4,82E-05 |
| BINO | 0,001120754 | INDX | -0,000529039 | MARK | 0,002248326 | UNTR | 0,00156 |
| BLUE | -0,000200802 | INTA | -0,000295592 | MDRN | -0,001425336 | VOKS | 0,00019 |
| BNBR | 0,035952987 | JECC | 0,000163008 | MFMI | 0,000193753 | ZBRA | 0,00014 |
| CAKK | 0,000685604 | JTPE | -0,001555248 | MLIA | 0,000612725 | | |
| CCSI | 0,000230376 | KBLI | -0,000127511 | NTBK | -0,000892615 | | |
| CTTH | -0,001695577 | KBLM | 0,000491882 | PADA | -0,000153406 | | |

Tabel 3. Market Return Stock Variance-Covariance Value

| Kode Saham | Beta | Kode Saham | Beta | Kode Saham | Beta | Kode Saham | Beta |
|------------|---------|------------|---------|------------|---------|------------|---------|
| AMFG | 1,00307 | DYAN | -1,3898 | KIAS | 2,72304 | SCCO | -0,5464 |
| APII | 0,04433 | GPSO | 1,74039 | KOBX | 1,82239 | SINI | -1,2781 |
| ARKA | 0 | HOPE | 0,67344 | KOIN | 2,90987 | SKRN | 1,00339 |
| ARNA | 0,63078 | IBFN | -6,0442 | KONI | 3,17913 | SOSS | -0,6027 |
| ASGR | 0,73773 | ICON | -0,193 | KUAS | -0,0763 | SPTO | 0,34759 |
| ASII | 0,72379 | IKAI | 0 | LABA | 0,7902 | TIRA | -2,2591 |
| BHIT | -0,0662 | IMPC | -0,0644 | LION | -1,2419 | TOTO | 0,08114 |
| BINO | 1,88565 | INDX | -0,8901 | MARK | 3,78277 | UNTR | 2,63081 |

| | | | | | | | |
|------|---------|------|---------|------|---------|------|------|
| BLUE | -0,3378 | INTA | -0,4973 | MDRN | -2,3981 | VOKS | 2,56 |
| BNBR | 60,4903 | JECC | 0,27426 | MFMI | 0,32599 | ZBRA | 1,83 |
| CAKK | 1,15352 | JTPE | -2,6167 | MLIA | 1,0309 | | |
| CCSI | 0,3876 | KBLI | -0,2145 | NTBK | -1,5018 | | |
| CTTH | -2,8528 | KBLM | 0,82758 | PADA | -0,2581 | | |

Tabel 4. Beta Risk Coefficient Value of Each Stock

4. Determination of Stocks for Portfolio Candidates with DEA

To determine the stocks that are used as portfolio candidates, we look at which stocks are efficient using the Data Development Analysis (DEA) method. The technical efficiency value of CRS (TR CCR) is obtained by completing the DEA-CCR model and the technical efficiency value of VRS (TE CCR) is obtained by completing the DEA-BCC model. While the efficiency scale (SE) is obtained from the comparison of TE CRS with TE VRS. With the help of DEAP Software, the technical efficiency values in the DEA-CCR model, the DEA-BCC model and the efficiency scale are shown in Table 5. The technical efficiency value for each DMU in the DEA-CCR and DEA-BCC models shows whether or not the performance of a DMU is efficient. A DMU is said to be efficient if its efficiency value is equal to one, if it is less than one, the DMU is said to be inefficient.

| KODE | TE CRS | TE VRS | SE | KODE | TE CRS | TE VRS | SE |
|------|--------|--------|-------|------|--------|--------|-------|
| AMFG | 1.000 | 1.000 | 1.000 | KBLM | 0.810 | 1.000 | 0.810 |
| APII | 0.566 | 1.000 | 0.566 | KIAS | 0.811 | 1.000 | 0.811 |
| ARKA | 0.459 | 1.000 | 0.459 | KOBX | 1.000 | 1.000 | 1.000 |
| ARNA | 0.752 | 1.000 | 0.752 | KOIN | 1.000 | 1.000 | 1.000 |
| ASGR | 0.746 | 1.000 | 0.746 | KONI | 0.563 | 1.000 | 0.563 |
| ASII | 1.000 | 1.000 | 1.000 | KUAS | 0.536 | 1.000 | 0.536 |
| BHIT | 0.534 | 1.000 | 0.534 | LABA | 0.830 | 1.000 | 0.830 |
| BINO | 1.000 | 1.000 | 1.000 | LION | 0.843 | 1.000 | 0.843 |
| BLUE | 1.000 | 1.000 | 1.000 | MARK | 0.674 | 1.000 | 0.674 |
| BNBR | 1.000 | 1.000 | 1.000 | MDRN | 0.487 | 1.000 | 0.487 |
| CAKK | 0.673 | 1.000 | 0.673 | MFMI | 0.600 | 1.000 | 0.600 |
| CCSI | 1.000 | 1.000 | 1.000 | MLIA | 1.000 | 1.000 | 1.000 |
| CTTH | 0.875 | 1.000 | 0.875 | NTBK | 0.686 | 1.000 | 0.686 |
| DYAN | 1.000 | 1.000 | 1.000 | PADA | 0.600 | 1.000 | 0.600 |
| GPSO | 0.801 | 1.000 | 0.801 | SCCO | 0.664 | 1.000 | 0.664 |
| HOPE | 0.767 | 1.000 | 0.767 | SINI | 1.000 | 1.000 | 1.000 |
| IBFN | 1.000 | 1.000 | 1.000 | SKRN | 0.452 | 1.000 | 0.452 |
| ICON | 0.749 | 1.000 | 0.749 | SOSS | 0.744 | 1.000 | 0.744 |
| IKAI | 0.461 | 1.000 | 0.461 | SPTO | 1.000 | 1.000 | 1.000 |
| IMPC | 0.383 | 1.000 | 0.383 | TIRA | 0.833 | 1.000 | 0.833 |
| INDX | 1.000 | 1.000 | 1.000 | TOTO | 0.554 | 1.000 | 0.554 |
| INTA | 0.578 | 1.000 | 0.578 | UNTR | 0.879 | 1.000 | 0.879 |
| JECC | 1.000 | 1.000 | 1.000 | VOKS | 0.915 | 1.000 | 0.915 |
| JTPE | 0.646 | 1.000 | 0.646 | ZBRA | 0.601 | 1.000 | 0.601 |
| KBLI | 0.617 | 1.000 | 0.617 | | | | |

Tabel 5. Efficiency Value of Each Stock

In the DEA-CCR model, there are 15 DMUs that demonstrate efficient performance (with an efficiency score of 1). These DMUs are AMFG, ASII, BINO, BLUE, BNBR, CCSI, DYAN, IBFN, INDX, JECC, KOBX, KOIN, MLIA, SINI, and SPTO. In the DEA-BCC

model, it can be observed that the efficiency scores of each DMU are much closer to one compared to the DEA-CCR model. This indicates that the performance efficiency evaluation in the DEA-BCC model is much closer to being efficient. For instance, in the DEA-CCR model, the efficiency score of DMU APII is 0.566, while in the DEA-BCC model, its efficiency score is 1.000. The same occurs with DMUs NTBK and PADA, which suggests that their performance is efficient. Therefore, more efficient DMUs are found in the DEA-BCC model. Meanwhile, scale efficiency (SE) is used to determine whether a DMU is operating optimally. If the efficiency score is less than one, the DMU has not yet operated optimally. If the VRS technical efficiency is greater than the scale efficiency, it indicates that changes in efficiency are influenced by pure technical efficiency. Conversely, if VRS technical efficiency is smaller than the scale efficiency, changes in efficiency are driven by scale efficiency. From Table D.5, it is shown that the DMUs operating optimally are AMFG, ASII, BINO, BLUE, BNBR, CCSI, DYAN, IBFN, INDX, JECC, KOBX, KOIN, MLIA, SINI, and SPTO. These 15 DMUs are considered as potential portfolio candidates.

Determining Fund Proportion

In the single index model, the first step is to calculate the ERB (excess return to beta) value. To calculate ERB, data on the risk-free asset return is required. In this study, the average monthly SBI interest rate during the research period is used, with an average return of 0.65%. The following table shows the ERB values of the 15 stocks, ranked from highest to lowest.

| KODE SAHAM | ERB | Ci | ERBi/ Ci |
|------------|----------|----------|----------|
| IBFN | 1,048988 | 0,00165 | 635,8851 |
| DYAN | 0,19647 | 0,024576 | 7,994276 |
| SINI | 0,195888 | 0,033581 | 5,83332 |
| BLUE | 0,18345 | 0,074167 | 2,473465 |
| INDX | 0,170878 | 0,085192 | 2,005802 |
| SPTO | 0,162965 | 0,120338 | 1,354225 |
| ASII | 0,156954 | 0,125769 | 1,247959 |
| JECC | 0,148464 | 0,127492 | 1,164501 |
| CCSI | 0,145672 | 0,129675 | 1,123357 |
| MLIA | 0,142909 | 0,131365 | 1,087878 |
| AMFG | 0,141012 | 0,132281 | 1,066005 |
| BINO | 0,125345 | 0,131492 | 0,95325 |
| KOBX | 0,123392 | 0,130987 | 0,942013 |
| KOIN | 0,109111 | 0,129646 | 0,841608 |
| BNBR | 0,0262 | 0,117579 | 0,222829 |

Table 6. ERB and Ci Value of Each Stock

The optimal portfolio will consist of stocks with high ERB values. The Cut-off Point (C*) is used as the threshold for a stock to be included in the portfolio, with the highest Ci value being the cut-off. The highest Cut-off Point (C*) is 0.1323, corresponding to the stock AMFG (Asahimas Flat Glass, Tbk). From the table, it can be seen that 11 stocks meet the criteria for inclusion in the optimal portfolio. These stocks are IBFN, DYAN, SINI, BLUE, INDX, SPTO, ASII, JECC, CCSI, MLIA, and AMFG.

After identifying the 11 stocks selected for the optimal portfolio, the next step is to determine the proportion (w_i) to be invested in each stock. The investment proportions for each stock in the portfolio are as follows.

| KODE SAHAM | NAMA PERUSAHAAN | PROPORSI SAHAM |
|------------|--------------------------------|----------------|
| IBFN | Intan Baru Prana Tbk. | 7% |
| DYAN | Dyandra Media International Tb | 8% |
| SINI | Singaraja Putra Tbk. | 3% |
| BLUE | Berkah Prima Perkasa Tbk. | 17% |
| INDX | Tanah Laut Tbk | 7% |
| SPTO | Surya Pertiwi Tbk. | 32% |
| ASII | Astra International Tbk. | 9% |
| JECC | Jembo Cable Company Tbk. | 4% |
| CCSI | Communication Cable Systems In | 5% |
| MLIA | Mulia Industrindo Tbk | 5% |
| AMFG | Asahimas Flat Glass Tbk. | 3% |

Tabel 7. Optimal Portfolio Share Proportion

The portfolio composed of 11 stocks provides a monthly return of 0.0211213 with a standard deviation of 0.026621. This portfolio is still above the risk-free return rate of 0.0065 per month.

CONCLUSIONS

Based on the analysis using the DEA-CCR and DEA-BCC models, 16 stocks were found to have optimal efficiency from the 49 stocks studied. Of these, 11 stocks were selected to form the optimal portfolio, including IBFN, DYAN, SINI, BLUE, INDX, SPTO, ASII, JECC, CCSI, MLIA, and AMFG, with varying fund allocations. This portfolio generated a return of 0.031213 per month with a standard deviation of 0.308529, which is higher than the market's expected return of 0.026621 and remains above the risk-free rate of 0.0065. For future research, the DEA model oriented toward input-output can be further developed, while potential investors are advised to carefully choose stocks to achieve optimal results.

ACKNOWLEDGMENTS

We would like to express our deepest gratitude to LPPM Universitas Respati Yogyakarta (Unriyo) for the support and funding provided for this research. The support from LPPM Unriyo has been instrumental in ensuring the successful completion of this research. We also extend our heartfelt thanks to all members of the research team for their hard work and dedication in completing this study. Your cooperation and commitment are greatly appreciated. Furthermore, we would like to thank the Indonesia Stock Exchange for providing easy access to the essential data needed for this research. We hope that the results of this study will offer significant benefits to the advancement of knowledge and the investment world

REFERENCES

- [1] Zvi. Bodie, Alex. Kane, and A. J. Marcus, *Essentials of investments*. McGraw-Hill/Irwin, 2013.
- [2] "Fabozzi-Gupta-Mar".
- [3] E. J. Elton and M. J. Gruber, "Modern Portfolio Theory, 1950 to date," *J Bank Financ*, vol. 21, no. 11, pp. 1743–1759, 1997, doi: [https://doi.org/10.1016/S0378-4266\(97\)00048-4](https://doi.org/10.1016/S0378-4266(97)00048-4).

- [4] V. W. Sujarweni *et al.*, "Introduction to Management: Development of Management Thought; Principles of Management; Basic Concepts of Management; Management Process Systems; Operations Management; Management Functions; Strategic Management; International Management; Business Ethics," 2024, Indonesia's Great Children.
- [5] Ph. D. , M. C. Prof. Jogiyanto Hartono, *Portfolio and Investment Analysis Module Approach (2nd Edition)*. Yogyakarta: Andi Publisher, 2022.
- [6] H. Markowitz, "Portfolio Selection," *J Finance*, vol. 7, no. 1, pp. 77–91, Mar. 1952, doi: <https://doi.org/10.1111/j.1540-6261.1952.tb01525.x>.
- [7] M. Fuad and H. Agustanto, "Analysis of Portfolio Compilation Using the Data Envelopment Method," 2016.
- [8] W. F. Sharpe, "Capital Asset Prices: A Theory of Market Equilibrium Under Conditions Of Risk," *J Finance*, vol. 19, no. 3, pp. 425–442, Sep. 1964, doi: <https://doi.org/10.1111/j.1540-6261.1964.tb02865.x>.
- [9] N. P. M. Mahayani and A. A. G. Suarjaya, "Determination of Optimal Portfolio Based on Markowitz Model in Infrastructure Company in Indonesia Stock Exchange," *E-Journal of Management*, Udayana University., Vol. 8, No. 5, P. 3057, Mar. 2019, doi: 10.24843/ejmunud.2019.v08.i05.p17.
- [10] A. Charnes, W. W. Cooper, and E. Rhodes, "Measuring the Efficiency Of Decision-Making Units," *Eur J Oper Res*, Vol. 2, No. 6, Pp. 429–444, 1978, doi: [https://doi.org/10.1016/0377-2217\(78\)90138-8](https://doi.org/10.1016/0377-2217(78)90138-8).
- [11] L. Ode Saidi, H. Budiman, Jufra, and Aswani, "Perbandingan Pembentukan Portofolio Optimal Model Markowitz Dan Model Indeks Tunggal (Single Index Model) On Index Stocks Idx30," 2022. [Online]. Available: <http://ojs.uho.ac.id/index.php/JMKS>
- [12] E. F. Fama and K. R. French, "Common Risk Factors in The Returns on Stocks and Bonds," *J Financ Econ*, Vol. 33, No. 1, Pp. 3–56, 1993.
- [13] A. K. Adiputra, P. E. E. Christmawan, and N. E. Meilaretasya, "Optimal portfolio analysis of stocks listed on IDX BUMN 20 Indonesia Stock Exchange," in *Proceeding of National Conference on Accounting & Finance*, 2022, Pp. 377–383.
- [14] L. F. Israwan, B. Surarso, and F. Frikhin, "Implementation of CCR Data Envelopment Analysis (DEA) Model on Regional Financial Efficiency Measurement," *Jurnal Sistem Informasi Bisnis*, Vol. 6, No. 1, P. 76, May 2016, Doi: 10.21456/Vol6iss1pp76-83.
- [15] R. D. Banker, A. Charnes, and W. W. Cooper, "Some Models for Estimating Technical And Scale Inefficiencies In Data Envelopment Analysis," *Manage Sci*, Vol. 30, No. 9, Pp. 1078–1092, 1984.
- [16] V. W. Sujarweni, "Business & Economic Research Methodology," 2015, Yogyakarta: Pustaka Baru Press..
- [17] A. Damodaran, "Equity Risk Premiums (ERP): Determinants, Estimation and Implications-The 2012 Edition." [Online]. Available: <http://ssrn.com/abstract=2027211> Electronic copy available at: <https://ssrn.com/abstract=2027211>
- [18] J. Merton, "A Quantitative Analysis of Financial Performance and EPA Environmental Measures in the US Automotive Market," Colorado Technical University, 2021.
- [19] D. Nyoman and S. Werastuti, "Formation of Optimal Portfolio through Decision-Making Units (Dmu) Efficiency Approach that Generates Relative Efficiency Score Based on Single Index Model."
- [20] S. A. Ross, "Ross, SA/Westerfield, RW/Jaffe, JF," *Corporate Finance*, vol. 5, 1999.